

Sudoku Puzzle with Definite Integrals  
(Basic Integrals, Integration by Parts, Area Under a Curve)  
A Puzzle by David Pleacher

Solve the 36 integral problems below and place the answer in the corresponding cell (labeled A, B, C, ... Y, Z, a, b,.. i, j).

Your answers should be integers from 1 to 9 inclusive.

Then solve the resulting SUDOKU puzzle.

The rules of Sudoku are simple.

Enter digits from 1 to 9 into the blank spaces.

Every row must contain one of each digit.

So must every column, and so must every 3x3 square.

Each Sudoku has a unique solution that can be reached logically without guessing.

$$A. \int_0^3 (3 - 2x + x^2) dx =$$

$$B. 3 \int_0^2 (2 - x)^2 dx =$$

$$C. \frac{9}{2} \int_{-3}^{-1} \left( \frac{1}{x^2} - \frac{1}{x^3} \right) dx =$$

$$D. \int_1^3 \left( \frac{3}{2}x^2 - \frac{9}{2}x + 3 \right) dx =$$

$$E. 3 \int_{-1}^1 (2x^2 - x^3) dx =$$

$$F. \int_0^2 (2 + x) dx =$$

$$G. \int_0^3 t^2 dt =$$

H. Determine the area bounded by the x-axis, the function  $y = \frac{5}{2\sqrt{2x+1}}$ ,  $x = 0$ , and  $x = 4$ .

I. Determine the area bounded by the x-axis, the function  $y = \frac{3x}{\sqrt{2x^2+1}}$ ,  $x = 0$ , and  $x = 2$ .

$$\text{J. } \int_0^4 \frac{(x^3 - 2) dx}{8} =$$

$$\text{K. } \int_1^4 \frac{dx}{\sqrt{x}} =$$

$$\text{L. } \int_0^{\frac{\pi}{2}} 9 \cos x dx$$

$$\text{M. } \int_0^{\frac{\pi}{6}} \frac{14 \sin 2x}{\cos^2 2x} dx$$

$$\text{N. } \int_{-1}^1 \left( \frac{9(x+1)^2}{8} \right) dx =$$

O. Determine the total area bounded by the curve  $y = x^3 - 4x$  and the x-axis.

$$\text{P. } \int_0^2 \left( \frac{3\sqrt{4x+1}}{13} \right) dx =$$

$$\text{Q. } \int_1^4 \frac{3}{4} \left( \sqrt{x} + \frac{1}{\sqrt{x}} \right) dx =$$

$$\text{R. } \int_0^2 \frac{27}{100}(x+1)(2x+6) dx =$$

$$\text{S. } \int_1^e \ln x dx =$$

T. Determine the area under one arch of the curve  $y = \sin(x)$ .

U. Determine the area bounded by the x-axis, the function  $y = x^3 + 2x$ ,  $x = 0$ , and  $x = 2$ .

V. Determine the area bounded by the x-axis, the function  $y = 2x + 3$ ,  $x = 0$ , and  $x = 1$ .

W. Determine the area between the curve  $y = \frac{1}{\sqrt{x}}$ , the x-axis, and the lines  $x = 1$   
and  $x = 4$ .

$$\text{X. } \int_1^2 \frac{9}{49}(2x+1)^2 dx =$$

$$\text{Y. } \int_0^{\ln 6} e^x dx =$$

$$\text{Z. } \int_{-1}^1 5\sqrt[3]{x^2} dx =$$

a. Determine the area contained between the x-axis and one arch of the curve  $y = 3 \cos(3x)$ .

b. Determine the area between the curve  $x = 6(1 - y^2)$  and the y-axis.

c. Determine the area bounded by  $y^2 = x - 1$  and  $y = x - 3$ . Then double your answer.

$$\text{d. } \int_1^2 (2x+5) dx =$$

$$\text{e. } \int_1^{e^4} \frac{dx}{x} =$$

f. Determine the area bounded by  $x = -2$ ,  $x = 0$ ,  $y = x^3$ , and  $y = -x$ .

$$\text{g. } \int_0^{\pi} 3 \cos^2 x \sin x \, dx$$

$$\text{h. } \int_0^{\sqrt{3}} \frac{6x \, dx}{\sqrt{4-x^2}} =$$

$$\text{i. } \int_1^2 3x^2 \, dx =$$

$$\text{j. } \int_1^e \frac{10 \ln x \, dx}{x} =$$



## Solution to the Sudoku With Definite Integrals Puzzle

$$A = 9$$

$$B = 8$$

$$C = 5$$

$$D = 1$$

$$E = 4$$

$$F = 6$$

$$G = 9$$

$$H = 5$$

$$I = 3$$

$$J = 7$$

$$K = 2$$

$$L = 9$$

$$M = 7$$

$$N = 3$$

$$O = 8$$

$$P = 1$$

$$Q = 5$$

$$R = 9$$

$$S = 1$$

$$T = 2$$

$$U = 8$$

$$V = 4$$

$$W = 2$$

$$X = 3$$

$$Y = 5$$

$$Z = 6$$

$$a = 2$$

$$b = 8$$

$$c = 9$$

$$d = 8$$

$$e = 4$$

$$f = 6$$

$$g = 2$$

$$h = 6$$

$$i = 7$$

$$j = 5$$

9	7	2	6	8	5	4	1	3
1	4	6	3	2	9	5	8	7
3	8	5	7	4	1	6	2	9
2	9	7	4	3	6	8	5	1
6	5	3	9	1	8	2	7	4
8	1	4	5	7	2	9	3	6
5	6	1	2	9	7	3	4	8
7	3	9	8	5	4	1	6	2
4	2	8	1	6	3	7	9	5