

## **CLUES:**

- 1. All students are located at integral coordinates in the xy-plane. The x-coordinates belong to the set {-2, -1, 0, 1, 2}, and the y-coordinates belong to the set {-1, 0, 1, 2, 3}.
- 2. Abel is seated on the line which is normal to the curve  $f(x) = x^2 2x + 4$  at the point (1, 3).
- 3. Brahmagupta sits on the line normal to the curve  $y = x^5 x^4 + 1$  at x = 1.
- 4. Cantor is located on the line tangent to the curve  $y = -x^2 + 10x 25$  at the point (5, 0).
- 5. Descartes is seated on the line normal to  $y = -x x^2$  at x = -1.
- 6. Euclid sits on the line tangent to  $y = x^3 + x^2$  at (3, 36).
- 7. Fermat is located on the line tangent to  $y = \sqrt{x^2 + 5}$  at the point (-2,3).
- 8. The curve  $y = ax^2 + bx + c$  passes through the point (2, 4) and is tangent to the line y = x + 1 at (0, 1). Determine values for a, b, and c. Gauss sits at the point (-b-c, 4a).
- 9. Hardy sits at one of the points on the curve  $y = 2x^3 3x^2 12x + 20$  where the tangent is parallel to the x-axis.
- 10. Jacobi is seated on the line tangent to the graph of  $y = 2x^3 3x^2 12x + 21$  at x = 2.
- 11. Klein is located on the tangent line to  $y = 3x^2 x$  at x = 1.
- 12. Leibniz sits on the line which is tangent to the curve  $y = 4x^2 22x + 35$  at the point (3, 5).
- 13. Mandelbrot sits at the point on the curve  $y = (x+2)^2$  where the normal to that curve is parallel to the y-axis.
- 14. Newton's seat is collinear with those of Gauss and Cantor.
- 15. Determine the values of a, b, and c where the curves  $y = x^2 + ax + b$  and  $y = cx + x^2$  have a common tangent line at (-1,0). Pythagoras sits at the point (b, a+c).
- 16. Riemann sits on the line normal to the curve  $y = x^2 3x + 2$  at x = 1.
- 17. The line tangent to a curve at a point  $(x_1, y_1)$  is y = 2x 2. The normal to that curve at the same point passes through (11, -5). Taylor sits at the point  $(x_1, y_1)$ .

- 18. Venn's seat is collinear with those of Brahmagupta and Zeno.
- 19. Wallis is seated on the line tangent to  $y = 4 3x x^2$  at the point (2, -6).
- 20. Zeno is located on the line tangent to  $y = \frac{2x+5}{x^2-3}$  at x = 1.

## **CLUE Worksheet**

For each problem, write down all possible answers from the given domain and range.

NAME	CLUE	Possible Ordered Pairs for the Seat				
	1					
Abel	2	(1, -1)	(1, 0)	(1, 1)	(1, 2)	(1, 3)
Brahmagupta	3	(-1, 3)	(0, 2)	(1, 1)	(2, 0)	
Cantor	4	(-1, 0)	(-2, 0)	(0, 0)	(1, 0)	(2, 0)
Descartes	5	(-1, 0)	(0, -1)	(-2, 1)		
Euclid	6	(2, 3)				
Fermat	7	(1, 1)	(-2, 3)			
Gauss	8	(-2, 1)				
Hardy	9	(2, 0)				
Jacobi	10	(-2, 1)	(-1, 1)	(0, 1)	(1, 1)	(2, 1)
Klein	11	(1, 2)				
Leibniz	12	(1, 1)	(0, -1)	(2, 3)		
Mandelbrot	13	(-2, 0)				
Newton	14	(2, -1)	(0, -1)			
Pythagoras	15	(0, 2)				
Riemann	16	(0, -1)	(1, 0)	(2, 1)		
Taylor	17	(1, 0)				
Venn	18	(1, -1)				
Wallis	19	(1, 1)				
Zeno	20	(0, 1)				
	]			1	1	1