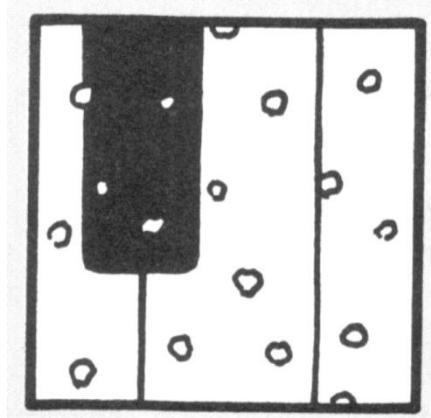


Turvy for Integration -- Answer Key

By David Pleacher



Here is the title right-side-up: Cookie crumbs on a piano

Here is the title upside-down: Abe Lincoln walking by a tall fence in a snowstorm

INTEGRAL PROBLEM

1. Evaluate $\int \left(\frac{1}{x^4} + \frac{1}{x^2} + x^{10} \right) dx$

2. $\int 4 \left(\frac{1}{x} + x^{\frac{2}{5}} \right)^2 dx =$

3. $\int \frac{x^2 - 9}{x+3} dx =$

4. $\int (\sin x - 3 \cot x \sin x) dx =$

5. $\int \left(2x^{-\frac{3}{7}} + \frac{5}{\sin^2 x} \right) dx =$

6. $\int \csc^2 x \cos x dx =$

7. $\int \frac{d}{dx} (3x^{-2} + \tan x - 4) dx =$

CORRESPONDING ANSWER

W. $-\frac{x^{-3}}{3} - x^{-1} + \frac{x^{11}}{11} + C$

K. $-\frac{4}{x} + 20x^{\frac{2}{5}} + \frac{20}{9}x^{\frac{9}{5}} + K$

R. $\frac{x^2}{2} - 3x + C$

P. $-\cos x - 3 \sin x + C$

Y. $\frac{7}{2}x^{\frac{4}{7}} - 5 \cot x + C$

G. $-\csc x + C$

U. $3x^{-2} + \tan x + K$

INTEGRAL PROBLEM

8. $\int \cos(2x)\sqrt{\sin(2x)} dx =$

9. $\int \frac{x}{\sqrt{1-x^2}} dx =$

10. Given that $g'(x) = (\sin x)(5+5\cos x)^3$,
find $g(x)$ if $g(0)=0$

11. $\int 8x(x^2+7)^3 dx =$

12. $\int \frac{x^2}{(2x^3-12)^4} dx =$

13. $\int \frac{(2+\sqrt{x})^6}{\sqrt{x}} dx =$

14. $\int \left(3-\frac{1}{x}\right)^{-2} \left(\frac{1}{x^2}\right) dx =$

15. $\int \frac{\cos x}{(2-3\sin x)^4} dx =$

16. $\int \frac{x}{\cos^2(3x^2)} dx =$

17. $\int \frac{4x^3-3}{(x^4-3x)^2} dx =$

18. $\int \cos x \cos(\sin x) dx =$

19. $\int 3x \tan(3x^2) \sec^2(3x^2) dx =$

CORRESPONDING ANSWER

B. $\frac{1}{3} \sin^{\frac{3}{2}}(2x) + C$

C. $-\sqrt{1-x^2} + C$

A. $-\frac{1}{20}(5+5\cos x)^4 + 500$

M. $(x^2+7)^4 + C$

I. $\frac{-1}{18(2x^3-12)^3} + C$

L. $\frac{2}{7} \left(2+x^{\frac{1}{2}}\right)^7 + C$

F. $-\left(3-\frac{1}{x}\right)^{-1} + K$

T. $\frac{1}{9}(2-3\sin x)^{-3} + C$

N. $\frac{1}{6} \tan(3x^2) + C$

S. $\frac{-1}{(x^4-3x)} + C$

O. $\sin(\sin x) + C$

E. $\frac{1}{4} \tan^2(3x^2) + C$