

Name \_\_\_\_\_

## Algebraic Atrocities

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### Statement

### Correction

1.  $\frac{3}{a} + \frac{3}{b} = \frac{3}{a+b}$

$$\frac{3}{a} + \frac{3}{b} = \frac{3a+3b}{ab}$$

2.  $\frac{a+b}{c+d} = \frac{a}{c} + \frac{b}{d}$

$$\frac{a+b}{c+d} = \frac{a}{c+d} + \frac{b}{c+d}$$

3.  $\frac{a+b}{c} = \frac{a}{c} + \frac{b}{c}$

TRUE

4.  $\frac{a}{b+c} = \frac{a}{b} + \frac{a}{c}$

$$\frac{a}{b+c} = \frac{a}{b+c} \text{ (cannot split up)}$$

5.  $\frac{10t+u}{10u+v} = \frac{t}{v}$

$$\frac{10t+u}{10u+v} = \frac{10t+u}{10u+v} \text{ (cannot simplify)}$$

6.  $\frac{a}{b} = \frac{a^2}{b^2}$

$$\frac{a}{b} = \frac{a}{b} \text{ (cannot square)}$$

7.  $\frac{a+b}{b} = a$

$$\frac{a+b}{b} = \frac{a}{b} + 1 \text{ (cannot divide with +)}$$

8.  $\frac{1}{a+b} + (a+b)^2 = a+b$

$$\frac{1}{a+b} \times (a+b)^2 = a+b$$

9.  $2a^{-1} = \frac{-1}{2a}$

$$2a^{-1} = \frac{2}{a}$$

10.  $a^{-2} = -a^2$

$$a^{-2} = \frac{1}{a^2}$$

11.  $(a-b)^2 = a^2 - b^2$

$$(a-b)^2 = a^2 - 2ab + b^2$$

12.  $(a+b)^2 = a^2 + b^2$

$$(a+b)^2 = a^2 + 2ab + b^2$$

13.  $(a+b)^3 = a^3 + b^3$        $(a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$
14.  $\sqrt{a^2} = a$        $\sqrt{a^2} = |a|$  ( $\sqrt{\phantom{x}}$  is only positive root)
15.  $\sqrt{a^2 + b^2} = a + b$        $\sqrt{a^2 + b^2} = \sqrt{a^2 + b^2}$  (cannot be simplified)
16.  $\sqrt{a^2 - b^2} = a - b$        $\sqrt{a^2 - b^2} = \sqrt{a^2 - b^2}$  (cannot be simplified)
17.  $\sqrt{a+b} = \sqrt{a} + \sqrt{b}$        $\sqrt{a+b} = \sqrt{a+b}$  (cannot be simplified)
18.  $\frac{1}{3}(-6)^3 = -2^3$        $\frac{1}{3}(-6)^3 = -72$
19.  $a^{\frac{2}{3}} = \frac{a^2}{a^3}$        $a^{\frac{2}{3}} = \sqrt[3]{a^2}$
20.  $\frac{\sin a}{a} = \sin(1)$        $\frac{\sin a}{a} = \frac{\sin a}{a}$  but  $\lim_{a \rightarrow 0} \left( \frac{\sin a}{a} \right) = 1$
21.  $\frac{\sin 2a}{a} = \sin(2)$        $\frac{\sin 2a}{a} = \frac{\sin 2a}{a}$  or  $\frac{2 \sin a \cos a}{a}$
22.  $\sin(2A) = 2 \sin(A) \cos(A)$        $\sin(2A) = 2 \sin(A) \cos(A)$
23.  $\sin(A+B) = \sin(A) + \sin(B)$        $\sin(A+B) = \sin(A) \cos(B) + \cos(A) \sin(B)$
24.  $\cos(2A) = 2 \cos(A)$        $\cos(2A) = \cos^2(A) - \sin^2(A)$
25.  $\cos(A+B) = \cos(A) + \cos(B)$        $\cos(A+B) = \cos(A) \cos(B) - \sin(A) \sin(B)$
26.  $\log(a+b) = \log(a) + \log(b)$        $\log(a \times b) = \log(a) + \log(b)$
27. If  $a+b=0$ , then either  $a=0$  or  $b=0$       If  $a+b=0$ , then  $a=-b$
28. If  $x(x-2)=24$ , then either  $x=24$  or  $x-2=24$       NO! Only works if set = 0
29.  $a(bc) = (ab)(ac)$        $a(bc) = (ab)(c)$  (not distributive)
30. If  $\log(a) = b$ , then  $a = \frac{b}{\log}$       If  $\log(a) = b$ , then  $a = 10^b$

31. If  $\sin(a) = b$ , then  $a = \frac{b}{\sin}$       If  $\sin(a) = b$ , then  $a = \text{Sin}^{-1}(b)$
32. If  $\cos(a) = b$ , then  $a = \frac{b}{\cos}$       If  $\cos(a) = b$ , then  $a = \text{Cos}^{-1}(b)$
33. If  $\tan(a) = b$ , then  $a = \frac{b}{\tan}$       If  $\tan(a) = b$ , then  $a = \text{Tan}^{-1}(b)$
34.  $\text{Sin}^{-1}(x) = \frac{1}{\csc(x)}$        $\text{Sin}^{-1}(x) = \text{Csc}^{-1}\left(\frac{1}{x}\right)$  or  $\sin(x) = \frac{1}{\csc(x)}$
35.  $\text{Tan}^{-1}(x) = \frac{1}{\cot(x)}$        $\text{Tan}^{-1}(x) = \text{Cot}^{-1}\left(\frac{1}{x}\right)$  or  $\tan(x) = \frac{1}{\cot(x)}$
36.  $\text{Cos}^{-1}(x) = \frac{1}{\sec(x)}$        $\text{Cos}^{-1}(x) = \text{Sec}^{-1}\left(\frac{1}{x}\right)$  or  $\cos(x) = \frac{1}{\sec(x)}$
37.  $\text{Sin}^{-1}(x) = \frac{1}{\sin(x)}$        $\text{Sin}^{-1}(x)$  means Arcsin(x) but  $(\sin(x))^{-1} = \frac{1}{\sin(x)}$