

I. Definitions

1. Write the definition for a *relation*.

2. What is the definition of the *period* of a trigonometric function?

3. Write the definition of the *sine* function.

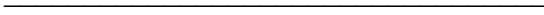
4. Write the general equation for an *exponential function*.

5. Write the definition of the *median* of a set of data.

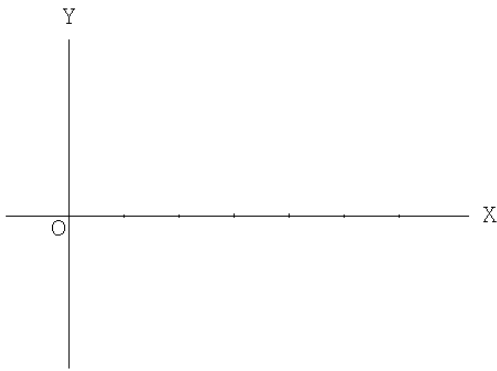
6. Write the general form of a *sinusoidal function*.

II. Sketch the graphs of each of the following in the spaces provided.

7. A normal distribution.



8. The cosecant function.

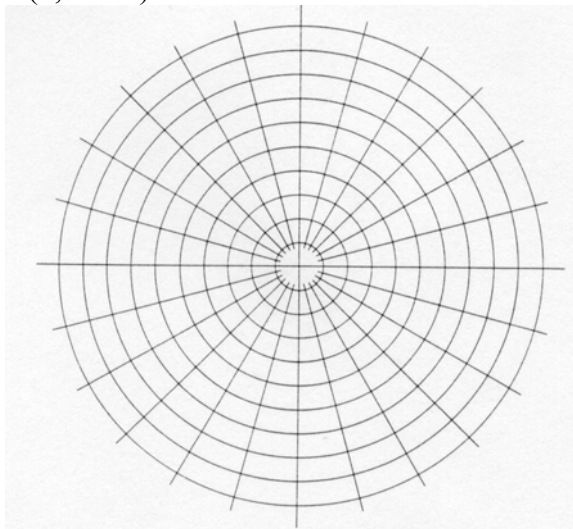


9. Graph the following points on the polar coordinate graph paper below:

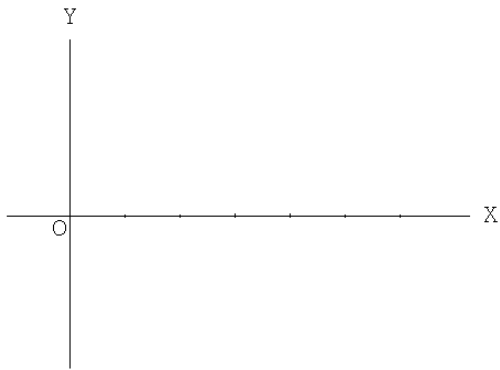
A $(-4, -45^\circ)$

B $(5, 300^\circ)$

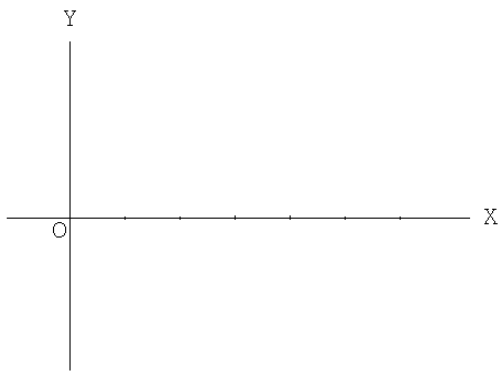
C $(4, -150^\circ)$



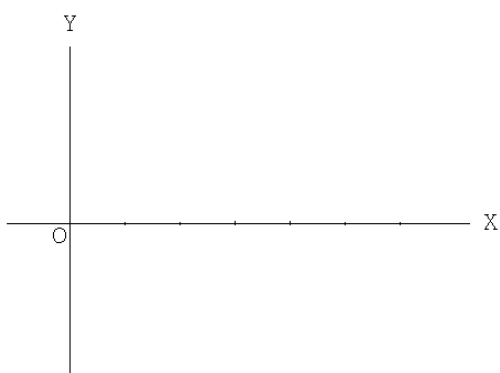
10. The tangent function.



11. $y = 3 \sin(2x)$



12. $y = \text{Cos}^{-1}x$



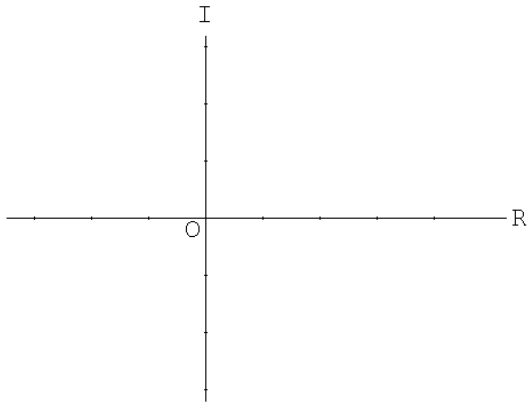
13. A rose curve with three petals.

14. Graph the following on the complex number plane:

(A) $2 - 3i$

(B) $-3 + 2i$

(C) $-1 - 3i$



III. Different kinds of functions have different properties.

15. State the trigonometric identity involving the squares of sines and cosines.

16. State the double angle property for **cos (2x)**.

17. State the property of the logarithm of the quotient of two numbers.

18. State the *Law of Cosines*.

19. State the probability that event A occurs and that event B occurs.

20. State *Heron's formula*.

IV. Proofs are essential in mathematics.

21. Prove by *mathematical induction* that the sum of the first n positive odd integers is n^2 .

$$\text{Prove: } 1 + 3 + 5 + \dots + (2n - 1) = n^2$$

22. Prove the following identity:

$$\cos^4 \theta - \sin^4 \theta = 1 - 2\sin^2 \theta$$

23. Prove the following identity:

$$\frac{\tan^2 x + 6 \tan x + 5}{\sec^2 x - 2} = \frac{\tan x + 5}{\tan x - 1}$$

23. Prove the following identity:

$$(1 + \sin \theta)(1 - \sin \theta) = \cos^2 \theta$$

V. The word *inverse* is an important concept in mathematics.

- _____ 24. Determine the additive inverse of 4.
- _____ 25. Determine the inverse function of $y = 3x + 12$
- _____ 26. Determine the inverse tangent of -1
(that is, evaluate $\text{Tan}^{-1}(-1)$)

VI. Multiple Choice

- _____ 27. A geometric series has $t_1 = 7$ and $r = 3$. Determine the value of the fifteenth term.
- (A) 472,969 (C) 14,348,907
(B) 33,480,783 (D) 1.0044×10^8
- _____ 28. The number 818 is a term in the arithmetic sequence 19, 36, 53, ... Which term is it?
- (A) 53 (B) 47 (C) 48 (D) 43
- _____ 29. The binomial $(h - j)^{20}$ is expanded as a binomial series. The term with j^7 is
- (A) $77520 h^{13} j^7$ (B) $125970 h^{13} j^7$
(C) $-77520 h^{13} j^7$ (D) $-125970 h^{13} j^7$
- _____ 30. If $\vec{a} = 8\vec{i} - 5\vec{j}$ and $\vec{b} = 6\vec{i} + 7\vec{j}$, determine $\vec{a} + \vec{b}$ in terms of its components.
- (A) $14\vec{i} + 2\vec{j}$ (B) $14\vec{i} - 2\vec{j}$ (C) $48\vec{i} - 35\vec{j}$
(D) $-2\vec{i} + 12\vec{j}$ (E) None of these
- _____ 31. Rewrite $7 - 2i$ in trigonometric form (Polar form).
- (A) $\sqrt{53}(\cos 344.1^\circ + i \sin 344.1^\circ)$ (B) $3\sqrt{5}(\cos 344.1^\circ + i \sin 344.1^\circ)$
(C) $3\sqrt{5}(\cos 15.9^\circ + i \sin 15.9^\circ)$ (D) $\sqrt{53}(\cos 15.9^\circ + i \sin 15.9^\circ)$
(E) None of these
- _____ 32. A function having the **period π** is
- (A) $y = 2 \sin(\theta)$ (B) $y = \frac{1}{2} \sin(\theta)$
(C) $y = \sin\left(\frac{1}{2}\theta\right)$ (D) $y = \sin(2\theta)$

_____ 33. Simplify: $\frac{1 - \sin^2 \theta}{\sin \theta} \cdot \frac{1}{\cos^2 \theta}$

- (A) $\sin(\theta)$ (B) $\csc(\theta)$ (C) $\cot(\theta)$ (D) $\cos^2 \theta$

_____ 34. If $\cos \theta = -\frac{3}{5}$ and $\tan \theta = -\frac{4}{3}$ then $\sin \theta =$

- (A) $\frac{3}{4}$ (B) $-\frac{4}{5}$ (C) $\frac{4}{5}$ (D) $-\frac{3}{4}$

VII. Short Answer

_____ 35. Solve for x: $x = \sin^{-1}\left(\frac{\sqrt{2}}{2}\right)$

_____ 36. Solve for θ : $2 \cos^2 \theta - 5 \cos \theta + 2 = 0$ for $0^\circ \leq \theta < 360^\circ$

_____ 37. Solve for θ : $2 \cos^2 \theta - 1 = 0$ for $0^\circ \leq \theta < 360^\circ$

_____ 38. Convert $\frac{7\pi}{15}$ radians to degrees.

_____ 39. Determine the value of $\sec(-2555^\circ)$

_____ 40. Which trigonometric functions are positive in the fourth quadrant?

_____ 41. In which quadrants is the cosecant negative?

_____ 42. A window is 23 feet above the ground. What angle will a 27-foot ladder make with the house when it is touched to the bottom of the window?

_____ 43. Determine the measure of the smallest angle in a 5-12-13 right triangle.

VIII. Multiple Choice

_____ 44. If θ is an acute angle, express $\sin \theta$ in terms of $\cos \theta$.

- (A) $\sqrt{\cos^2 \theta - 1}$ (B) $\sqrt{1 - \cos^2 \theta}$
(C) $1 - \cos \theta$ (D) $1 - \cos^2 \theta$

_____ 45. If $\sin(B) = \cos(B)$, what is the measure of $\angle B$?

- (A) $\frac{\pi}{4}$ (B) $\frac{\pi}{2}$ (C) $\frac{\pi}{3}$ (D) $\frac{\pi}{6}$

_____ 46. In $\triangle ABC$, side $a = 3$ inches, $\sin A = .1$, and $\sin B = .2$; what is the length of side b ?

- (A) 0.6 (B) 6 (C) 1.5 (D) 15

_____ 47. The expression $\log \sqrt{xy}$ is equivalent to

- (A) $2(\log x + \log y)$ (C) $\frac{1}{2}(\log x \cdot \log y)$
(B) $\frac{1}{2}(\log x + \log y)$ (D) $2 \log x \cdot \log y$

_____ 48. The inverse of $y = \log_2 x$ is

- (A) $y = x^2$ (B) $x = y^2$ (C) $x = 2^y$ (D) $y = 2^x$

_____ 49. In $\triangle ABC$, if side $a = 8$, side $b = 9$, and side $c = 10$, what is the measure of $\angle C$?

- (A) 36.8° (B) 65.4° (C) 71.8° (D) 89.4°

_____ 50. Given $\triangle ABC$ with side $a = 91.6$ inches, side $c = 24.19$ inches, and $m\angle B = 37^\circ$, Determine the area of the triangle.

- A) 1107.9 square inches B) 1333.5 square inches
C) 1769.6 square inches D) 666.8 square inches
E) None of these

_____ 51. In a baseball park, the distance from home plate to a point A in straightaway centerfield is 400 feet. Determine the distance from A to first base. (Straightaway centerfield is an extension of the line drawn from home plate through second base. The distance between consecutive bases is 90 feet).

- (A) 66.2 feet (B) 135 feet (C) 342 feet (D) 378 feet

_____ 52. If $\log_x \left(\frac{1}{4}\right) = 2$ then $x =$

- (A) 2 (B) -2 (C) $-\frac{1}{2}$ (D) $\frac{1}{2}$

_____ 53. Determine the value of i^{352}

- (A) 1 (B) -i (C) i (D) -1

_____ 54. Determine the resultant of the two given displacements below:

8 units at a bearing of 90° followed by 6 units along a bearing of 210°

- (A) 7.2 units at a bearing of 136°
(B) 51.9 units at a bearing of 46°
(C) 7.2 units at a bearing of 46°
(D) Can not be determined
(E) None of the above

_____ 55. Simplify $\frac{2}{3-i}$

- (A) $\frac{3+i}{2}$ (B) $\frac{6-2i}{3-i}$ (C) $\frac{3+i}{4}$ (D) $\frac{3+i}{5}$

_____ 56. In $\triangle PEG$, $p = 6$ cm, $e = 7$ cm, and $g = 11$ cm. Then $m\angle G =$

- A) 115.3° B) 98.6° C) 64.7° D) 18.27°
E) Not possible (no such triangle)

_____ 57. Compute the number of combinations of 8 items taken 3 at a time.

- (A) 56 (B) 336 (C) 40,320 (D) 6

IX. Problems (Short Answer)

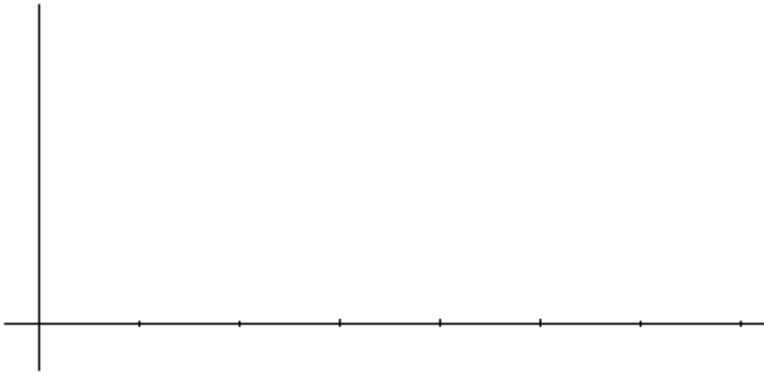
- _____ 58. Compute ${}_6P_3$
- _____ 59. If a card is drawn at random from a standard deck of cards, calculate the probability of drawing a diamond.
- _____ 60. In how many ways could you arrange 4 books on a shelf if there are 9 books from which to choose?
- _____ 61. There are 9 boys and 4 girls on the Handley golf team. The coach selects a group of 5 at random. What is the probability that the group consists of 3 boys and 3 girls?
- 62 – 64. Handley's Softball team, Boys' Track team, and Girls' Tennis team all play on Saturday. The probability that the track team will win is 0.6; the probability that the softball team will win is 0.5; and the probability that the tennis team will win is 0.8.
- _____ 62. What is the probability that all three will win?
- _____ 63. What is the probability that all three will lose?
- _____ 64. What is the probability that all at least one of them will win?
- _____ 65. On the mall at Apple Blossom, you were stunned to find your Precalculus teacher operating a table with the following game:
You pay \$1.00 and then pick a card at random from a standard deck of 52 cards.
If the card is an ace, you win \$4.00.
If the card is a face card, you win \$2.00.
If the card is anything else, you win nothing.
What is your mathematical expectation?
- _____ 66. Mr. P has 5 sport jackets, 5 pairs of trousers, and 310 hideous ties. How many different outfits (1 tie, 1 jacket, and 1 pair of pants) could he choose from if he selects a jacket, a tie, and a pair of pants at random?

_____ 67. Winchester's favorite *Elvis* restaurant, *Red, Hot, and Blue*, offers three types of ribs (*Sweet Ribs, Dry Ribs, and Wet Ribs*) and four Memphis-style sandwiches (*Pulled Pork, Pulled Chicken, Beef Brisket, and Ribwich Combo*). In how many different ways can you select one of the Ribs meals **OR** one of the sandwiches?

68 – 73. Given the following data:

<u>x</u>	<u>Frequency</u>
3	9
4	8
5	6
6	3
7	4

(histogram) 68. Plot a histogram of the frequency distribution.



_____ 69. Determine the **mean** for the set of data.

_____ 70. Determine the **median** for the set of data.

_____ 71. Determine the **mode** for the set of data.

_____ 72. Determine the **variance** for the set of data.

_____ 73. Determine the **standard deviation** for the set of data.

74 – 77. In 2001, 1,276,320 students took the SAT. The mean for the math SAT was 514 with a standard deviation of 113. Suppose that Matt E. Matics made a score of 640.

_____ 74. How many standard deviations is Matt's score above the mean?

_____ 75. What percent of the students made below Matt's score of 640?

_____ 76. How many of the 1,276,320 students scored higher than Matt?

_____ 77. What percent of the students scored between 490 and 680 ?

_____ 78. Transform the following to Cartesian coordinates and simplify.

$$r = 2 \sin \theta$$

_____ 79. Transform the following to polar coordinates:

$$y = x^2$$

_____ 80. Transform the parametric equations to a Cartesian equation by eliminating the parameter.

$$\begin{aligned}x &= 2t - 1 \\y &= 3t + 1\end{aligned}$$