

Do not write on this paper! Do all work on your own paper.

I. Basic Theorems and Proofs

1. Write out all three forms of the Law of Cosines for  $\triangle KAT$ .
2. Write out the Law of Sines for  $\triangle PEG$ .
3. Write out the formula for determining the area of a triangle if you are given:
  - A. the lengths of the three sides  $j$ ,  $a$ , and  $m$  of  $\triangle JAM$ .
  - B. the lengths of two sides  $q$  and  $e$  and the measure of  $\angle D$  of  $\triangle QED$ .
  - C. the lengths of the base  $b$  and the altitude  $h$  of  $\triangle BET$ .
4. Develop (Prove) the formula for the area of a triangle if you are given the lengths of two sides of the triangle and the measure of the included angle.

II. Multiple Choice

5. Given  $\triangle ABC$  with  $m\angle B = 34^\circ$ ,  $m\angle A = 90^\circ$ , and  $c = 14.7$  cm. Then  $b =$   
A) 17.7 cm      B) 9.92 cm      C) 16.6 cm      D) 8.81      E) 22.14 cm
6. In  $\triangle CAM$ ,  $m\angle M = 137^\circ$ ,  $a = 31.6$  ft, and  $c = 42.8$  ft. Then  $m =$   
A) 21.8 ft      B) 65.7 ft      C) 38.8 ft      D) 69.3 ft      E) 72.1 ft
7. In  $\triangle MEG$ ,  $m = 28$  cm,  $e = 12$  cm, and  $g = 13$  cm. The measure of the *smallest* angle is  
A)  $17.51^\circ$       B)  $18.27^\circ$       C)  $24.2^\circ$       D)  $137.5^\circ$   
E) Not possible (no such triangle)
8. . In  $\triangle PEG$ ,  $p = 6$  cm,  $e = 7$  cm, and  $g = 11$  cm. Then  $m\angle G =$   
A)  $115.3^\circ$       B)  $98.6^\circ$       C)  $64.7^\circ$       D)  $18.27^\circ$   
E) Not possible (no such triangle)

III. Free Response (SHOW ALL WORK!!)

9. Determine the area of  $\triangle MRP$  if  $m = 10$  in,  $p = 6$  in, and  $m\angle R = 46^\circ$ .
10. Determine the area of  $\triangle PAM$  if  $m = 11$  in,  $p = 7$  in, and  $a = 9$  in.
11. In  $\triangle MAY$ , you are given the measures of  $\angle M$ ,  $\angle A$ , and side  $y$ . Explain thoroughly how you would determine the measures of the other three parts of the triangle.
12. In  $\triangle XYZ$ ,  $m\angle X = 27^\circ$ ,  $x = 4$  cm, and  $y = 5$  cm. Determine the length of side  $z$ .
13. In  $\triangle ABC$ ,  $m\angle A = 127^\circ$ ,  $a = 5$  cm, and  $b = 7$  cm. Determine the length of side  $c$ .
14. In  $\triangle ABC$ ,  $m\angle B = 64^\circ$ ,  $a = 6$  cm, and  $m\angle A = 56^\circ$ . Solve for the missing three parts of the triangle.
15. The angles of elevation to an airplane from two points A and B on level ground are  $52^\circ$  and  $66^\circ$ , respectively. The points A and B are 5 miles apart, and the airplane is east of both points in the same vertical plane. Determine the altitude of the plane.